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## List of Principal Notation

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| $f_s$  | sampling frequency   |
| $T_s$  | sampling period  |
| $\omega$   | radian frequency (rad/s)   |
| $f$  | frequency (Hz) or normalized frequency( $f/f_s$ )  |
| $t$  | continuous time or normalized discrete-time (with respect to the sampling period $t/T_s$ ) |
| $k$  | normalized discrete time ( $t/T_s$ )   |
| $u(t), y(t)$   | plant input and output   |
| $y^*(t+d+1)$   | tracking reference   |
| $r(t)$   | reference or external excitation   |
| $e(t)$   | discrete time Gaussian white noise   |
| $q^{-l}$   | shift (delay) operator ( $q^{-l}y(t) = y(t-l)$ )   |
| $s, z$   | complex variables ( $z = e^{j\omega T_s}$ )  |
| $A(q^{-l}), B(q^{-l}), C(q^{-l})$                            | polynomials in the variable $q^{-l}$   |
| $d$  | delay of the discrete-time system (integer)  |
| $\hat{A}(t, q^{-l}), \hat{B}(t, q^{-l}), \hat{C}(t, q^{-l})$ | estimation of polynomials $A, B, C$ at instant $t$   |
| $\hat{a}_i(t), \hat{b}_i(t), \hat{c}_i(t)$                   | estimated coefficients of polynomials $A, B, C$  |
| $H(q^{-l})$  | pulse transfer operator (discrete time systems)  |
| $H(z^{-l}), H(z)$  | discrete-time transfer functions   |
| $\tau$   | time delay of a continuous-time system   |
| $R(q^{-l}), S(q^{-l}), T(q^{-l})$                            | pulse transfer operators used in a RST digital controller                                  |
| $S_{xy}(s), S_{xy}(z^{-l})$                                  | sensitivity functions  |
| $P(z^{-l})$  | closed loop characteristic polynomial  |
| $\Delta M$   | modulus margin   |
| $\Delta \tau$  | delay margin   |
| $\theta$   | parameter vector   |
| $\hat{\theta}(t)$  | estimated parameter vector   |
| $\varphi(t), \Phi(\tau)$                                     | measurement / observation vector   |
| $F, F(t)$  | adaptation gain  |
| $\varepsilon^\circ(t), \varepsilon(t)$                       | <i>a priori</i> / <i>a posteriori</i> prediction error                                     |

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| $\varepsilon_{CL}^o(t), \varepsilon_{CL}(t)$ | closed loop <i>a priori / a posteriori</i> prediction error                    |
| $v^o(t), v(t)$                               | <i>a priori / a posteriori</i> adaptation error                                |
| $A, F$                                       | matrices   |
| $F > 0$                                      | positive definite matrix   |
| $t_R$  | rise time  |
| $t_S$  | settling time  |
| $M$  | maximum overshoot  |
| $\omega_o, \zeta$                            | natural frequency and damping factor for a continuous-time second-order system |
| $E\{\cdot\}$                                 | expectation  |
| $MV$   | mean value   |
| $var.$                                       | variance   |
| $\sigma$                                     | standard deviation   |
| $R(i)$                                       | auto-correlation or cross-correlation  |
| $RN(i)$                                      | normalized auto-correlation or cross-correlation                               |
| $t_{im}$                                     | maximum length of pulse in a PRBS  |
| $OL$   | open loop  |
| $CL$   | closed loop  |
| $BP$   | bandwidth  |
| AF-CLOE                                      | adaptive filtered closed loop output error                                     |
| ARMAX  | Auto-Regressive Moving Average with eXogenous input process                    |
| CLIM   | closed loop input matching   |
| CLOE   | closed loop output error   |
| CLOM   | closed loop output matching  |
| ELS  | extended least squares   |
| F-CLOE                                       | filtered closed loop output error  |
| GLS  | generalized least squares  |
| IVAM   | instrumental variable with auxiliary model                                     |
| OEAO   | output error with adaptive filtered observations                               |
| OEEPM  | output error with extended prediction model                                    |
| OEFC   | output error with fixed compensator  |
| OEFO   | output error with filtered observations  |
| PAA  | parameter adaptation algorithm   |
| PID  | proportional + integral + derivative controller                                |
| PRBS   | pseudo random binary sequence  |
| RLS  | recursive least squares  |
| RML  | recursive maximum likelihood   |
| RST  | two degrees of freedom digital controller                                      |
| X-CLOE                                       | extended closed loop output error  |

*Warning*

For sake of notation uniformity, we shall often use, in the case of linear systems with constant coefficients,  $q^{-1}$  notation both for the delay operator and the complex variable  $z^{-1}$ . The  $z^{-1}$  notation will be especially employed when an interpretation in the frequency domain is needed (in this case  $z = e^{-j\omega T_s}$ ).